

# CoE/EE460 Switching Theory

## Lecture 20

Washington University  
Spring 2001

<http://www.arl.wustl.edu/~lockwood/class/coe460/>

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## Announcements

- **Final Exam**
  - Time
    - Friday May 4, 2001
    - 10:30am - 12:30pm
  - Place
    - Regular classroom
  - Material
    - Comprehensive
      - Exams 1-2
      - Lectures 1-19
      - Homeworks 1-8
  - Closed Book
    - Three pages of Notes allowed
- **Homework 8:**
  - Due Today!
- **New Course**
  - Fall 2001
  - CS/COE535m :
    - Acceleration of Algorithms in Hardware
    - Now Cross-listed with Computer Engineering
    - Sign up today if interested.
  - Network Packet processing in VHDL

## Finite Automata

- Type of Finite State Machine
- Declares inputs to be:
  - Accepted -or-
  - Rejected
- Input :  $X$
- State :  $S$
- State Transitions :  $\delta$
- Initial State :  $S_0$
- Accepting States :  $A$

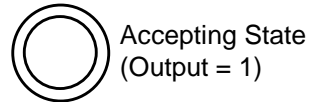
## Regular Language

- Regular Language
  - Alphabet: Set of symbols, e.g.  $\{0,1\}$  or  $\{a,b,c\}$ .
  - String: Sequence of symbols in the alphabet
    - $|S|$  = Length of String
    - Empty String:  $\epsilon$ 
      - $|\epsilon| = 0$
  - L: Language = Set of strings
    - $|L|$  = Size of language
    - Can be infinite

## Accepted Language / Accepting States

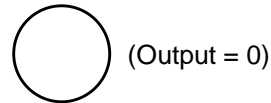
- Accepted Language

- Input = String
- Output = Accepted



- NFA : Non-disjoint next-state transitions

- Example Markov Chain



## DFA / NFA

- DFA : Deterministic Finite Automation

- Next state transitions well-defined

- NFA : Non-deterministic Finite Automation

- Multiple Next-state transitions possible
- Concise Description
- Non-physical implementation

- Example

- Graph with states that allow transition to non-singleton set of next-states.

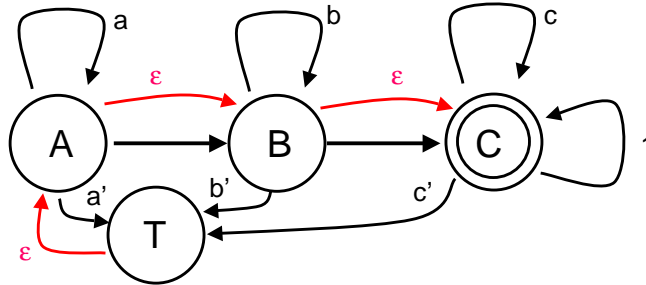
## Finite State Transitions

- **Deterministic Finite State Transitions**
  - Consider  $\delta(s,x) : X \times S \rightarrow S$
  - Where  $t = \delta(s,x) \in S$
- **Non-Deterministic Finite Automata**
  - Some  $\delta(s,x)$  map to multiple states
    - For all possible  $S$  in  $S$ ,  $X$  in  $X$
  - Consider  $\delta(s,x) : X \times S \rightarrow 2^S$
  - Where  $T = \delta(s,x) \in 2^S$
- **Complete Deterministic Finite Automata**
  - All possible  $\delta(S_i, X_k)$  map to single state
    - For all possible  $S$  in  $S$ ,  $X$  in  $X$

## NFAs

- Empty Input =  $\epsilon$
- **State Transitions**
  - Initial State
    - $\delta(A,a)=A$ ,  $\delta(A,a')=T$ ,  $\delta(A, \epsilon)=B$
  - Intermediate State
    - $\delta(B,b)=B$ ,  $\delta(B,b')=T$ ,  $\delta(B, \epsilon)=C$
  - Accepting State
    - $\delta(C,c)=C$ ,  $\delta(C,c')=T$ , Output = Accepted
  - Trap State
    - $T$

## Transitions of NFA



- Accepting Strings
  - abc
  - aaabbbbcc
  - ac

## Last Lecture Note of the Semester!

- Congratulations
  - You have worked hard throughout the semester!
- Where to go from here?
  - Classes next fall
    - CS/COE 535m: Acceleration of Algorithms in Hardware
  - Graduate School
    - Computer Engineering
    - Computer Science
    - EE
  - Industry
    - ASIC Design, Design Automation, Hardware Engineering
    - Xilinx, Altera, Intel, Cisco, Nortel, TI, Motorola, Others