

# Advanced Computer Systems Architecture

## Chip-Multiprocessors: Applications and Architectures

CSE 526M

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## Plan for Today

- Announcements
  - Palmer visit this Friday
  - Commentaries
  - Milestone reports
- Questions
- Today's discussion

## Project Logistics

- Dates
  - Today's date: Mar 16
  - End date: (**4.5 weeks later**) Thursday, April 15
- Weekly Milestones

|    |        |                           |
|----|--------|---------------------------|
| M1 | Mar 4  | Implementation 1          |
| M2 | Mar 18 | Implementation 2          |
| M3 | Mar 25 | Implementation 3          |
| M4 | Apr 1  | Implementation Wrap-up    |
| M5 | Apr 8  | Plan future work, Reports |
| M6 | Apr 15 | Presentations             |

## Objectives

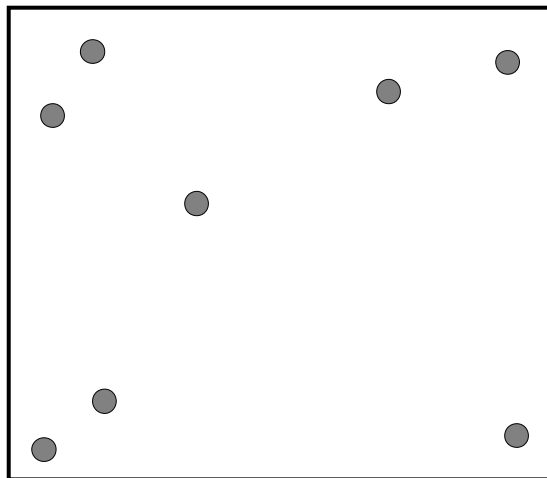
- Consider *performance optimization* in general terms
- Study a particular *performance evaluation* technique

## Outline

- Performance optimization
  - Case Study
  - Principles
- Worst-case execution time
  - Motivation
  - Technique

## Case Study: The N-body Problem

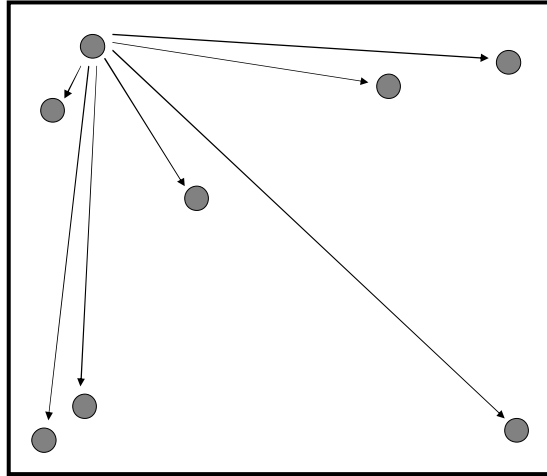
- Given masses, initial positions, and velocities: simulate interactions
- Each object could be a planet, e.g.



Resource: Bentley's Programming Pearls, 2<sup>nd</sup> edition

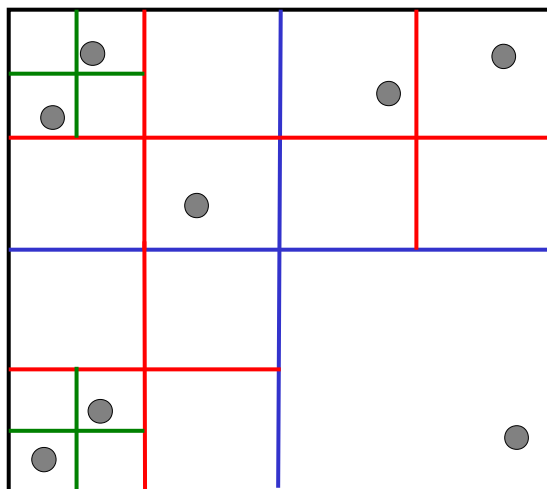
## Direct Implementation

- At each (small) time step, compute each objects movement
- Key point: each object influenced by all the others
- Complexity:  $O(n^2)$

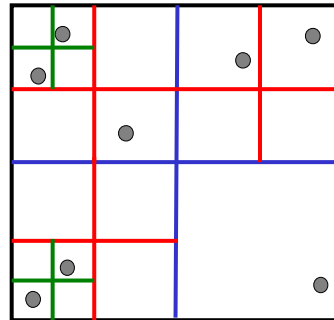
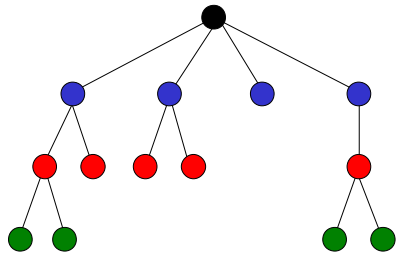


## Appel's Algorithmic Approach

- Construct a quadtree (for 2d)
- Treat *distant* clusters as a single point



## Quadtree Representation



- Leaves are objects
- Each non-leaf is a cluster
- Given a few constraints, each object is influenced by the clusters above it,  $O(n \log n)$

## System-wide Contributions

| Design Level           | Speedup    | Change  |
|------------------------|------------|---|
| Alg and Data Structure | 12         | Binary tree reduces $O(n^2)$ to $O(n \log n)$ |
| Alg Tuning             | 2          | Larger time steps                             |
| Data Structure         | 2          | Tree-specific D.S.                            |
| System-ind Code Tune   | 2          | Use single-precision integers                 |
| System-dep Code Tune   | 2.5        | Hand tuned critical function                  |
| Hardware               | 2          | F.P. accelerator                              |
| <b>Total</b>           | <b>400</b> |   |

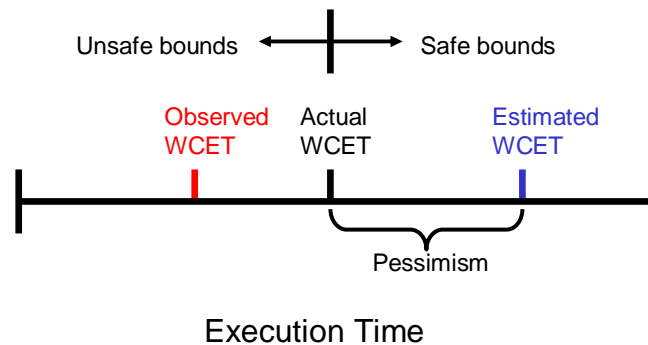
## Principles

- Dramatic performance available across all design levels in the system
- Improvements in algorithms have high impact, and can lead to additional improvements
- If you need a little speedup: choose the right level
- If you need a large speedup: work at multiple levels

## Worst-Case Execution Time (WCET)

- Networks are real time systems
  - Implementations must be both *functionally* and *temporally* correct
  - If service time exceeds inter-arrival time, the system will be unstable
- Minimum reliable performance *can* be stated in terms of worst-case conditions
  - Best effort routers
  - Beyond best effort: differentiated services

## WCET: Safety & Tightness



## WCET on Network Processors

- Challenges:
  - Implementations are software
  - Programs run on multithreaded multiprocessors
- Related real-time systems work
  - Studied recently
  - No work on *multithreading*

**Question:** How do you find a safe & tight worst-case bound?

## A Method for Multithreaded WCET Estimation

- Basic idea:
  - Use integer linear programming techniques to find the most expensive of all paths through a program's control-flow graph (CFG).
- Decidability restrictions on programs:
  - No unbounded loops
  - No dynamic data structures
  - No recursion
- Based on Implicit Path Enumeration (IPET)
  - Work by Steven Li, *et al.* from Princeton

## The Problem

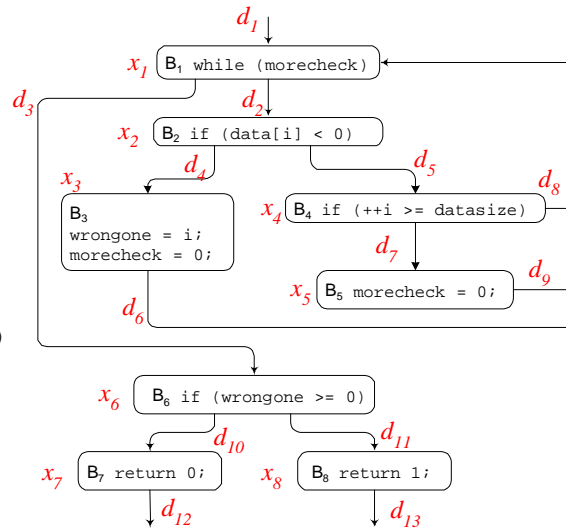
- Question 1
  - How long will one thread take to complete?
  - Assuming a simple, single issue processor
- *Question 2*
  - *How long will group of threads take to complete?*
  - *Assuming a single issue processor with 0-cycle context switches*
- Only considering worst-case throughput here

# Example

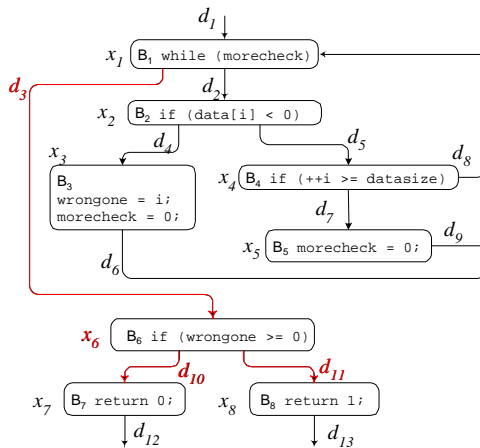
```

/*
morecheck = 1;
i = 0; datasize = 10;
wrongone = -1;
*/
while (morecheck) {
  if (data[i] < 0) {
    wrongone = i;
    morecheck = 0;
  }
  else
    if (++i >= datasize)
      morecheck = 0;
}
if (wrongone >= 0)
  return 0;
else
  return 1;

```



# Structural constraints



$$d_1 = 1$$

$$x_1 = d_1 + d_6 + d_8 + d_9 = d_2 + d_3$$

$$x_2 = d_2 = d_4 + d_5$$

$$x_3 = d_4 = d_6$$

$$x_4 = d_5 = d_7 + d_8$$

$$x_5 = d_7 = d_9$$

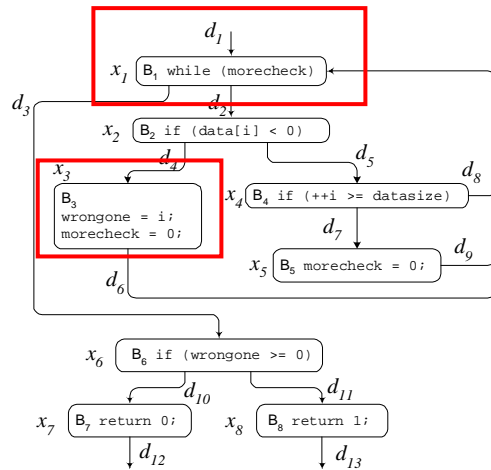
$$x_6 = d_3 = d_{10} + d_{11}$$

$$x_7 = d_{10} = d_{12}$$

$$x_8 = d_{11} = d_{13}$$

- Flow in = flow out

## Functional constraints



- Loop bound:

$$1d_1 \leq x_1 \leq 10d_1$$

- Additionally:

$$x_3 \leq 1d_1$$

## Problem Statement

- Assume each basic block has a constant cost  $c_i$
- The constraints bound the feasible  $\mathbf{x}_i$  values.
- Solve for WCET by maximizing the sum:

$$\text{Program Execution Time} = \sum_{i=1}^N c_i x_i$$

Subject to the structural and functional constraints

## Assignment

- Thursday (3/18)
  - Milestone 2
- Tuesday (3/23):
  - **Commentary:** *Hints for Computer System Design*, by Butler Lampson