Problem 1 (0 Points)
Tanenbaum, Problem 40 (Chapter 2).

Problem 2 (2 Points)

- Consider the case of two tasks \((N = 2)\) where the service demands are \(t(1) = 5\) and \(t(2) = 3\). What is the average response time for the two possible service orderings (i.e., job 1 then job 2 and job 2 then job 1)?

- Consider the more general case of \(N\) jobs with service demands of \(t(i), i=1:N\) where the service demands are strictly ordered; i.e., \(t(1) < t(2) < \ldots < t(N)\). Prove that SJF will result in the smallest average response time. HINT: Consider the average response time when Job \(i\) swaps service position with Job \(i-1\).

Problem 3 (4 Points)

We wish to derive the *equations of motion* for a workload that consists of \(N + 1\) jobs consisting of \(N\) type A jobs and one type B job being serviced by the simple scheduling scheme described below. Job type A has a CPU demand of \(a\) seconds, and job type B has a demand of \(b\) seconds. Furthermore, \(b\) is a large integer multiple of \(a\), and type A jobs arrive at fixed time points \(X, 2X, 3X, \text{ etc.}\) where \(X\) is a positive integer multiple of \(a\); i.e., \(X = ka\) where \(k\) is a positive integer.

In this system, type A jobs have a higher priority than the one type B job and will preempt (with 0 overhead) any type B job from the CPU.

a) Draw the space-time diagram (time runs to the right) for the case when \(a = 1, b = 10, k = 2,\) and \(N = 4\).

b) Derive an expression for the turnaround time and the queueing time of the type B job and each type A job. Here, you need to handle the general case of arbitrary \(N\) and \(k\) although subject to the constraints specified earlier; i.e., \(k\) is a positive integer, and \(b\) is a large integer multiple of \(a\).
Problem 4 (4 Points) [From Tanenbaum (modified)]

Suppose that a machine has 48-bit virtual addresses with a single-level page table and 32-bit physical addresses. Pages are 4 KB.

a) How many bits should be allocated for each of the page number and the offset fields in the virtual (logical) address? Explain.

b) How many entries are needed for the single-level page table?

c) How many pages would be needed for the page table?

d) If the program and data together fit in page 0 and the stack fits in the highest page, how many page table entries are needed for two-level paging if an equal number of bits are used to represent each part of the page number? Explain.

Problem 5 (0 Points)

Consider a buddy system and the address 011011110000.

a) If the block size associated with this address is 8 bytes, what is the binary address of the buddy?

b) What is the largest block size $N$ such that the above address still has a buddy? Explain.

Problem 6 (4 Points)

Consider a buddy system and the address 100100001000. Assume the largest block has $2^U$ bytes and the smallest block has $2^L$ bytes.

a) If the block size is 8 bytes, what is the binary address of the buddy?

b) What is the largest block size $N$ such that the above address still has a buddy? Explain.

c) Let $b_k(x)$ be the buddy of address $x$ with block size $2^k$. Write an expression for $b_k(x)$. Explain why the form of the expression is correct. If you can’t write the expression, then give the algorithm for computing $b_k(x)$.

d) Demonstrate that your expression in Part c is correct.
Problem 7 (6 Points)

Modify the ucontext-basic.c program so that it creates 4 instances of the childFiber thread that executes the algorithm shown below. The details are the following:

- The id of kth childFiber is k.
- The algorithm for each childFiber is:

  Display "BEGIN" followed by my id;
  Do 2 times {
    Sleep for 1 second;
    Yield to my neighbor thread;
    Display "RESUME" followed by my id;
  }
  Sleep for 1 second;
  If I am not thread 3 Then
    Yield to my neighbor thread;
  Else
    Yield to the main thread;
  End
  Display "END" followed by my id;

In the above algorithm, thread \((k + 1) \mod 4\) is the next neighbor of thread \(k\); i.e., the threads form a ring control structure. The id is the instance number; i.e., 0, 1, 2, or 3.

Submit the following:

a) Your source listing

b) The output of your program

c) A short explanation of why your output shows that your program is functioning properly.